

## Lab 9 – t-statistic practice

**Due Monday, April 7 at beginning of class**

**Problem 1 (Multiple Hypotheses)** You are measuring the thickness of books in millimeters and you find that in a sample of  $n = 15$  you have  $\bar{x} = 25$  and  $\hat{\sigma} = 3$ . There are two competing hypotheses for the true thickness,  $H_{0_1} : \mu = 22$  and  $H_{0_2} : \mu = 26.5$

- Find a t-statistic associated with each hypothesis
- Using your worksheet, find the critical values associated with 80%, 90%, and 95% confidence
- At what confidence levels would you reject  $H_{0_1}$ ? How about  $H_{0_2}$ ?
- Against which hypothesis do we have more evidence against?

**Problem 2 (Multiple Samples)** We are interested in determining the *proportion* of countries in which the average life expectancy is greater than 70 years. To this end, we collected two different samples:

- **Sample 1:** 11 countries had life expectancy greater than 70, 14 did not
- **Sample 2:** 14 countries had life expectancy greater than 70, 16 did not

We hypothesize that the true proportion of countries with LE greater than 70 is  $p_0 = 0.65$ . Use this information to answer the following

- Find the  $t$ -statistic associated with each of these samples
- Why can we not compare the  $t$ -statistics directly in this case to determine which sample provides more evidence against the null? Do the  $t$  statistics from each sample follow the same distribution?
- Determine for each sample at which confidence level from the critical value sheet in which we would reject  $H_0$ . Based on this, which sample provides more evidence against the null hypothesis?